

- 1 (a) Show that  $(x - 3)$  is a factor of  $f(x)$ , where  $f(x) = 2x^3 + 3x^2 - 23x - 12$ .  
(b) Hence express  $f(x)$  in its fully factorised form.
- 2 Factorise fully:  
(a)  $3a^3 - a^2 - 20a - 12$  (b)  $m^4 - m$
- 3  $t^3 - 5t^2 + kt - 6$  has value  $-2$  when  $t = 2$ . Find  $k$ .
- 4 Solve  $4x^3 - 9x^2 - 3x + 10 = 0$
- 5 Find the quotient and remainder when  $2x^3 + 6x - 12$  is divided by  $(x + 2)$ .
- 6 When the polynomial  $f(x) = 2x^3 + px^2 + qx + 5$  is divided by  $(x - 3)$  the remainder is  $-4$ .  
When  $f(x)$  is divided by  $(x - 1)$ , the remainder is  $-2$ .  
Find the values of  $p$  and  $q$ .
- 7 Show that the equation  $4x^3 - 5x - 14$  has a root between 1 and 2 and find this root correct to one decimal place.